The Michell Solution

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ϕ	$\sigma_{\mathbf{rr}}$	$\sigma_{\mathbf{r\theta}}$	$\sigma_{\theta\theta}$	$\mathbf{2\mu u_\theta}$	$\mathbf{2\mu u_r}$
$\mathbf{r^2}$	2	0	2	0	$(\kappa-1)r$
$\mathbf{r^2}\ln(\mathbf{r})$	$2\ln(r)+1$	0	$2\ln(r)+3$	$(\kappa+1)r\theta$	$(\kappa-1)r\ln(r)-r$
$\ln(\mathbf{r})$	$\frac{1}{r^2}$	0	$-\frac{1}{r^2}$	0	$-\frac{1}{r}$
θ	0	$\frac{1}{r^2}$	0	$-\frac{1}{r}$	0
$\mathbf{r}\theta\sin\theta$	$\frac{2\cos\theta}{r}$	0	0	$\frac{1}{2}\Big\{(\kappa-1)\theta\cos\theta-\sin\theta$ $-(\kappa+1)\ln(r)\sin\theta\Big\}$	$\frac{1}{2}\Big\{(\kappa-1)\theta\sin\theta$ $-\cos\theta+(\kappa+1)\ln(r)\cos\theta\Big\}$
$\mathbf{r}\ln(\mathbf{r})\cos\theta$	$\frac{\cos\theta}{r}$	$\frac{\sin\theta}{r}$	$\frac{\cos\theta}{r}$	$\frac{1}{2}\Big\{(\kappa+1)\theta\cos\theta-\sin\theta$ $-(\kappa-1)\ln(r)\sin\theta\Big\}$	$\frac{1}{2}\Big\{(\kappa+1)\theta\sin\theta$ $-\cos\theta+(\kappa-1)\ln(r)\cos\theta\Big\}$
$\frac{\cos\theta}{\mathbf{r}}$	$-\frac{2\cos\theta}{r^3}$	$-\frac{2\sin\theta}{r^3}$	$\frac{2\cos\theta}{r^3}$	$\frac{\sin\theta}{r^2}$	$\frac{\cos\theta}{r^2}$
$\mathbf{r}\theta\cos\theta$	$-\frac{2\sin\theta}{r}$	0	0	$\frac{1}{2}\Big\{-(\kappa-1)\theta\sin\theta$ $-\cos\theta-(\kappa+1)\ln(r)\cos\theta\Big\}$	$\frac{1}{2}\Big\{(\kappa-1)\theta\cos\theta$ $+\sin\theta-(\kappa+1)\ln(r)\sin\theta\Big\}$
$\mathbf{r}\ln(\mathbf{r})\sin\theta$	$\frac{\sin\theta}{r}$	$-\frac{\cos\theta}{r}$	$\frac{\sin\theta}{r}$	$\frac{1}{2}\Big\{(\kappa+1)\theta\sin\theta$ $+\cos\theta+(\kappa-1)\ln(r)\cos\theta\Big\}$	$\frac{1}{2}\Big\{-(\kappa+1)\theta\cos\theta$ $-\sin\theta+(\kappa-1)\ln(r)\sin\theta\Big\}$
$\frac{\sin\theta}{\mathbf{r}}$	$-\frac{2\sin\theta}{r^3}$	$\frac{2\cos\theta}{r^3}$	$\frac{2\sin\theta}{r^3}$	$-\frac{\cos\theta}{r^2}$	$\frac{\sin\theta}{r^2}$
$\mathbf{r^{n+2}}\cos\mathbf{n}\theta$	$-(n+1)(n-2)r^n\cos n\theta$	$n(n+1)r^n\sin n\theta$	$(n+1)(n+2)r^n\cos n\theta$	$(\kappa+n+1)r^{n+1}\sin n\theta$	$(\kappa-n-1)r^{n+1}\cos n\theta$
$\mathbf{r^n}\cos\mathbf{n}\theta$	$-n(n-1)r^{n-2}\cos n\theta$	$n(n-1)r^{n-2}\sin n\theta$	$n(n-1)r^{n-2}\cos n\theta$	$nr^{n-1}\sin n\theta$	$-nr^{n-1}\cos n\theta$
$\mathbf{r^{n+2}}\sin\mathbf{n}\theta$	$-(n+1)(n-2)r^n\sin n\theta$	$-n(n+1)r^n\cos n\theta$	$(n+1)(n+2)r^n\sin n\theta$	$-(\kappa+n+1)r^{n+1}\cos n\theta$	$(\kappa-n-1)r^{n+1}\sin n\theta$
$\mathbf{r^n}\sin\mathbf{n}\theta$	$-n(n-1)r^{n-2}\sin n\theta$	$-n(n-1)r^{n-2}\cos n\theta$	$n(n-1)r^{n-2}\sin n\theta$	$-nr^{n-1}\cos n\theta$	$-nr^{n-1}\sin n\theta$