

AS2070: Aerospace Structural Mechanics Module 3: Introduction to Fatigue and Failure

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Chapter 3 in Jr and Rethwisch (2012).

ELEMENTS OF FRACTURE MECHANICS



Chapters 1-3 in Kumar (2009).



Chapter 15 in Megson (2013)

1.1. Structure of Materials

Introduction



Types of crystal structures in metals Sparky (2013)

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Introduction



Types of crystal structures in metals Sparky (2013)



Crystal and Grain Structures New Technique Provides Detailed Views of Metals' Crystal Structure (2016). "Polycrystallinity"

1.1. Structure of Materials



1.2. Understanding the Stress-Strain Curve



1.2. Understanding the Stress-Strain Curve



1. Introduction

"Griffith Theory" of brittle fracture

- Theoretical fracture stress $\sim \frac{E}{5} \frac{E}{30}$ (steel $\sim \frac{E}{1000}$)
- Fracture occurs when $E_{strain} = E_{surface}$
- Crack propagates when $\frac{dE_{strain}}{dL} = \frac{dE_{surface}}{dL}$

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Ductile Fracture



Ductile Fracture Rajendran 2011

Sr. No	Brittle Fracture	Ductile Fracture
1.	It occurs with no or little plastic deformation.	It occurs with large plastic deformation.
2.	The rate of propagation of the crack is fast.	The rate of propagation of the crack is slow.
3.	It occurs suddenly without any warning.	It occurs slowly.
4.	The fractured surface is flat.	The fractured surface has rough contour and the shape is similar to cup and cone arrangement.
5.	The fractured surface appears shiny.	The fractured surface is dull when viewed with naked eye and the surface has dimpled appearance when viewed with scanning electron microscope.
6.	It occurs where micro crack is larger.	It occurs in localised region where the deformation is larger.

Ductile vs Brittle Fracture Rajendran 2011

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1. Introduction

...over 90% of mechanical failures are caused because of metal fatigue *What Is Metal Fatigue?* 2021...



The De Havilland Comet The deHavilland Comet Disaster 2019 [lecture]

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...over 90% of mechanical failures are caused because of metal fatigue *What Is Metal Fatigue?* 2021...



A more recent example (2021 United Airlines Boeing 777) DCA21FA085.Aspx n.d. [video] The De Havilland Comet The deHavilland Comet Disaster 2019 [lecture]

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Introduction



Simplistic picture of the introduction of a crack in a stretched specimen(Figure from sec 2.5 in Kumar 2009)

- Because of the crack, we assume $\sigma \approx 0$ in the triangles.
- Corresponding energy loss:

$$E_R = V_\Delta \times \left(\frac{\sigma^2}{2E}\right) = \frac{2a^2\lambda t\sigma^2}{E}.$$

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- For thin plates, $\lambda = \frac{\pi}{2}$. So, $E_R = \frac{\pi a^2 t \sigma^2}{E}$.
- The "creation" of a surface takes energy. We write this as,

 $E_S = 2(2at)\gamma = 4at\gamma.$







Introduction

(Ref: Sec. 8.4.2 in Sadd 2009)

Consider the following two cases. **Question**: Where will the point of peak stress occur? And which will have higher maximum stress?



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1.6. Modes of Fracture

Introduction



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